Test Booklet No.

Subject : Mathematics/Applied Mathematics
Code : 319 E
Medium : English

Test Booklet Code

C

(Do not open this Test Booklet until you are asked to do so)

*Time Allowed : **60** minutes*	*Maximum Marks : **200***	*Total Questions : **15+35+35***	*Number of questions to be answered : **15+25***

Kindly read the Instructions given on this Page and Back Page carefully before attempting this Question Paper.

Important Instructions for the Candidates :

1. This Question Paper contains **two sections** i.e. **Section A** and **Section B (B1** and **B2).**

   Section A has **15 questions** covering both i.e. **Mathematics and Applied Mathematics** which is **compulsory** for all candidates.

   Section B1 has **35 questions** (Q. No. 16 to 50) from **Mathematics** out of which **25 questions** need to be attempted.

   Section B2 has **35 questions** (Q. No. 51 to 85) purely from **Applied Mathematics** out of which **25 questions** need to be attempted.

   If a candidate answers more than **25** questions from **Section B1/B2**, the first **25** answered questions will be considered for evaluation.
2. When you are given the OMR Answer Sheet, fill in your particulars on it carefully with **blue/black** ball point pen only.
3. Use only Blue/Black Ball Point Pen for marking responses. Kindly select Mathematics (Q. No. 16 to 50) **OR** Applied Mathematics (Q. No. 51 to 85) very carefully for marking responses on the OMR Answer Sheet.
4. The CODE for this Test Booklet is **C**. Make sure that the CODE printed on the OMR Answer Sheet is the same as that on this Test Booklet. Also ensure that your Test Booklet No. and OMR Answer Sheet No. are exactly the same. In case of discrepancy, the candidate should immediately report the matter to the Invigilator for replacement of both the Test Booklet and the OMR Answer Sheet. No claim in this regard will be entertained after five minutes from the start of the examination.
5. Before attempting the question paper kindly check that this Test Booklet has total **28** pages and OMR Answer Sheet consists of one sheet. At the start of the examination within first five minutes, candidates are advised to ensure that all pages of Test Booklet and OMR Answer Sheet are properly printed and they are not damaged in any manner.
6. Each question has four options. Out of these four options choose the **MOST APPROPRIATE OPTION** and darken/blacken the corresponding circle on the OMR Answer Sheet with a Blue/Black Ball Point Pen.
7. Five (5) marks will be given for each correct answer. One (1) mark will be deducted for each incorrect answer. If more than one circle is found darkened/blackened for a question, then it will be considered as an incorrect answer. Unanswered questions will be given no mark.

P.T.O.

Name of the Candidate (in Capital Letters) : _____

Application Number (in figures) : _____

Roll Number (in figures) : _____

Centre of Examination (in Capital Letters) : _____

Candidate's Signature : _____ Invigilator's Signature : _____

Facsimile signature stamp of Centre Superintendent : _____

Section A (Compulsory)

1. The second order derivative of which of the following functions is 5^x ?

(1) $5^x \log_e 5$

(2) $5^x (\log_e 5)^2$

(3) $\dfrac{5^x}{\log_e 5}$

(4) $\dfrac{5^x}{(\log_e 5)^2}$

2. The degree of the differential equation $\left(1-\left(\dfrac{dy}{dx}\right)^2\right)^{3/2} = k\dfrac{d^2y}{dx^2}$ is :

(1) 1

(2) 2

(3) 3

(4) $\dfrac{3}{2}$

3. $\displaystyle\int \frac{\pi}{x^{n+1} - x}\, dx =$

(1) $\dfrac{\pi}{n} \log_e \left|\dfrac{x^n - 1}{x^n}\right| + C$

(2) $\log_e \left|\dfrac{x^n + 1}{x^n - 1}\right| + C$

(3) $\dfrac{\pi}{n} \log_e \left|\dfrac{x^n + 1}{x^n}\right| + C$

(4) $\pi \log_e \left|\dfrac{x^n}{x^n - 1}\right| + C$

4. The value of $\displaystyle\int_0^1 \frac{a - bx^2}{\left(a + bx^2\right)^2}\, dx$ is :

(1) $\dfrac{a-b}{a+b}$

(2) $\dfrac{1}{a-b}$

(3) $\dfrac{a+b}{2}$

(4) $\dfrac{1}{a+b}$

SPACE FOR ROUGH WORK

5. If A and B are symmetric matrices of the same order, then AB – BA is a :

(1) symmetric matrix (2) zero matrix

(3) skew symmetric matrix (4) identity matrix

6. If A is a square matrix of order 4 and $|A| = 4$, then $|2A|$ will be :

(1) 8 (2) 64 (3) 16 (4) 4

7. If $[A]_{3\times2}\,[B]_{x\times y} = [C]_{3\times1}$, then :

(1) $x = 1, y = 3$ (2) $x = 2, y = 1$ (3) $x = 3, y = 3$ (4) $x = 3, y = 1$

8. If a function $f(x) = x^2 + bx + 1$ is increasing in the interval [1, 2], then the least value of b is :

(1) 5 (2) 0 (3) – 2 (4) – 4

9. Two dice are thrown simultaneously. If X denotes the number of fours, then the expectation of X will be :

(1) $\frac{5}{9}$ (2) $\frac{1}{3}$ (3) $\frac{4}{7}$ (4) $\frac{3}{8}$

10. For the function $f(x) = 2x^3 - 9x^2 + 12x - 5$, $x \in [0, 3]$, match **List-I** with **List-II** :

List-I	**List-II**
(A) Absolute maximum value	(I) 3
(B) Absolute minimum value	(II) 0
(C) Point of maxima	(III) – 5
(D) Point of minima	(IV) 4

Choose the **correct** answer from the options given below :

(1) (A) - (IV), (B) - (II), (C) - (I), (D) - (III) (2) (A) - (II), (B) - (III), (C) - (I), (D) - (IV)

(3) (A) - (IV), (B) - (III), (C) - (II), (D) - (I) (4) (A) - (IV), (B) - (III), (C) - (I), (D) - (II)

SPACE FOR ROUGH WORK

11. An objective function $Z = ax + by$ is maximum at points (8, 2) and (4, 6). If $a \geq 0$ and $b \geq 0$ and $ab = 25$, then the maximum value of the function is equal to :

(1) 60 (2) 50

(3) 40 (4) 80

12. The area of the region bounded by the lines $x + 2y = 12$, $x = 2$, $x = 6$ and x-axis is :

(1) 34 sq units

(2) 20 sq units

(3) 24 sq units

(4) 16 sq units

13. A die is rolled thrice. What is the probability of getting a number greater than 4 in the first and the second throw of dice and a number less than 4 in the third throw ?

(1) $\frac{1}{3}$ (2) $\frac{1}{6}$ (3) $\frac{1}{9}$ (4) $\frac{1}{18}$

14. The corner points of the feasible region determined by

$x + y \leq 8,\ 2x + y \geq 8,\ x \geq 0,\ y \geq 0$

are A(0, 8), B(4, 0) and C(8, 0). If the objective function $Z = ax + by$ has its maximum value on the line segment AB, then the relation between a and b is :

(1) $8a + 4 = b$ (2) $a = 2b$

(3) $b = 2a$ (4) $8b + 4 = a$

15. If $t = e^{2x}$ and $y = \log_e t^2$, then $\frac{d^2y}{dx^2}$ is :

(1) 0 (2) 4t

(3) $\frac{4e^{2t}}{t}$ (4) $\frac{e^{2t}(4t-1)}{t^2}$

SPACE FOR ROUGH WORK

Section B1 (Mathematics)

16. For a square matrix $A_{n\times n}$

(A) $|\text{adj } A| = |A|^{n-1}$

(B) $|A| = |\text{adj } A|^{n-1}$

(C) $A(\text{adj } A) = |A|$

(D) $\left|A^{-1}\right| = \dfrac{1}{|A|}$

Choose the **correct** answer from the options given below :

(1) (B) and (D) only

(2) (A) and (D) only

(3) (A), (C) and (D) only

(4) (B), (C) and (D) only

17. If the random variable X has the following distribution :

X	0	1	2	otherwise
P(X)	k	2k	3k	0

Match **List-I** with **List-II** :

List-I	**List-II**
(A) k	(I) $\frac{5}{6}$
(B) $P(X < 2)$	(II) $\frac{4}{3}$
(C) E(X)	(III) $\frac{1}{2}$
(D) $P(1 \le X \le 2)$	(IV) $\frac{1}{6}$

Choose the **correct** answer from the options given below :

(1) (A) - (I), (B) - (II), (C) - (III), (D) - (IV)

(2) (A) - (IV), (B) - (III), (C) - (II), (D) - (I)

(3) (A) - (I), (B) - (II), (C) - (IV), (D) - (III)

(4) (A) - (III), (B) - (IV), (C) - (I), (D) - (II)

SPACE FOR ROUGH WORK

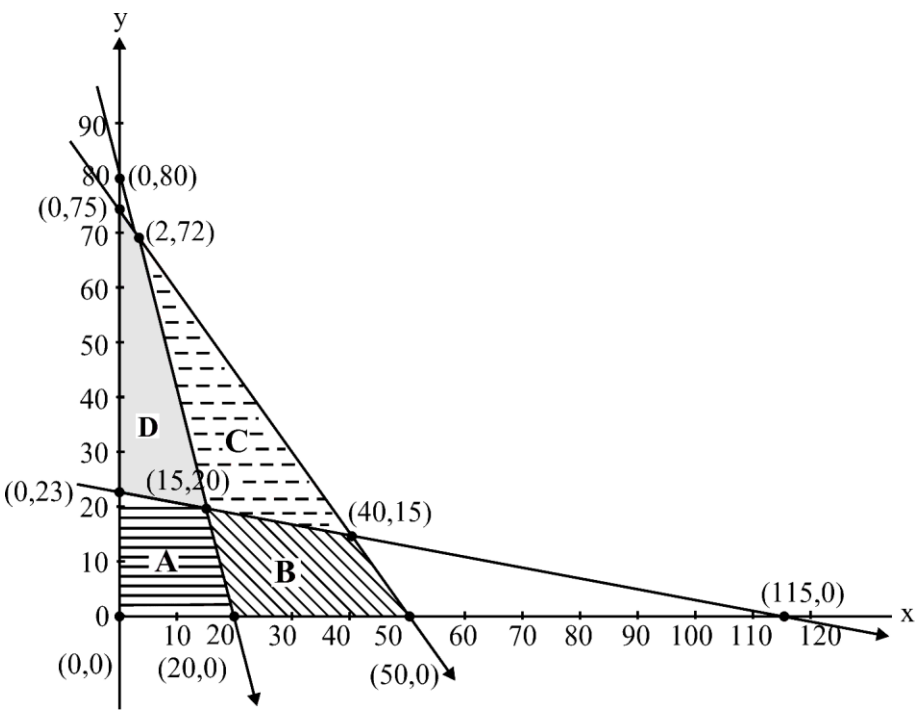
18. The matrix $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ is a :

(A) scalar matrix
(B) diagonal matrix
(C) skew-symmetric matix
(D) symmetric matrix

Choose the **correct** answer from the options given below :

(1) (A), (B) and (D) only
(2) (A), (B) and (C) only
(3) (A), (B), (C) and (D)
(4) (B), (C) and (D) only

19. The feasible region represented by the constraints $4x + y \geq 80$, $x + 5y \geq 115$, $3x + 2y \leq 150$, $x, y \geq 0$ of an LPP is



(1) Region A
(2) Region B
(3) Region C
(4) Region D

20. The area of the region enclosed between the curves $4x^2 = y$ and $y = 4$ is :

(1) 16 sq. units
(2) $\frac{32}{3}$ sq. units
(3) $\frac{8}{3}$ sq. units
(4) $\frac{16}{3}$ sq. units

SPACE FOR ROUGH WORK

21. $\int e^x \left(\frac{2x+1}{2\sqrt{x}} \right) dx =$

(1) $\frac{1}{2\sqrt{x}} e^x + C$

(2) $-e^x \sqrt{x} + C$

(3) $-\frac{1}{2\sqrt{x}} e^x + C$

(4) $e^x \sqrt{x} + C$

22. If f(x), defined by $f(x) = \begin{cases} kx+1 & \text{if} \quad x \le \pi \\ \cos x & \text{if} \quad x > \pi \end{cases}$ is continuous at $x = \pi$, then the value of k is :

(1) 0

(2) π

(3) $\frac{2}{\pi}$

(4) $-\frac{2}{\pi}$

23. If $P = \begin{bmatrix} -1 \\ 2 \\ 1 \end{bmatrix}$ and $Q = [2 \quad -4 \quad 1]$ are two matrices, then $(PQ)'$ will be :

(1) $\begin{bmatrix} 4 & 5 & 7 \\ -3 & -3 & 0 \\ 0 & -3 & -2 \end{bmatrix}$

(2) $\begin{bmatrix} -2 & 4 & 2 \\ 4 & -8 & -4 \\ -1 & 2 & 1 \end{bmatrix}$

(3) $\begin{bmatrix} 5 & 5 & 2 \\ 7 & 6 & 7 \\ -9 & -7 & 0 \end{bmatrix}$

(4) $\begin{bmatrix} -2 & 4 & 8 \\ 7 & 5 & 7 \\ -8 & -2 & 6 \end{bmatrix}$

SPACE FOR ROUGH WORK

24. $\Delta = \begin{vmatrix} 1 & \cos x & 1 \\ -\cos x & 1 & \cos x \\ -1 & -\cos x & 1 \end{vmatrix}$

(A) $\Delta = 2(1 - \cos^2 x)$

(B) $\Delta = 2(2 - \sin^2 x)$

(C) Minimum value of Δ is 2

(D) Maximum value of Δ is 4

Choose the **correct** answer from the options given below :

(1) (A), (C) and (D) only

(2) (A), (B) and (C) only

(3) (A), (B), (C) and (D)

(4) (B), (C) and (D) only

25. $f(x) = \sin x + \frac{1}{2} \cos 2x$ in $\left[0, \frac{\pi}{2}\right]$

(A) $f'(x) = \cos x - \sin 2x$

(B) The critical points of the function are $x = \frac{\pi}{6}$ and $x = \frac{\pi}{2}$

(C) The minimum value of the function is 2

(D) The maximum value of the function is $\frac{3}{4}$

Choose the **correct** answer from the options given below :

(1) (A), (B) and (D) only

(2) (A), (B) and (C) only

(3) (A), (B), (C) and (D)

(4) (B), (C) and (D) only

26. The direction cosines of the line which is perpendicular to the lines with direction ratios 1, – 2, – 2 and 0, 2, 1 are :

(1) $\frac{2}{3}, -\frac{1}{3}, \frac{2}{3}$

(2) $-\frac{2}{3}, -\frac{1}{3}, \frac{2}{3}$

(3) $\frac{2}{3}, -\frac{1}{3}, -\frac{2}{3}$

(4) $\frac{2}{3}, \frac{1}{3}, \frac{2}{3}$

SPACE FOR ROUGH WORK

27. Let X denote the number of hours you play during a randomly selected day. The probability that X can take values x has the following form, where c is some constant.

$$P(X = x) = \begin{cases} 0.1 & , \text{ if } x = 0 \\ cx & , \text{ if } x = 1 \text{ or } x = 2 \\ c(5 - x), & \text{ if } x = 3 \text{ or } x = 4 \\ 0 & , \text{ otherwise} \end{cases}$$

Match **List-I** with **List-II** :

List-I		List-II	
(A)	c	(I)	0.75
(B)	$P(X \le 2)$	(II)	0.3
(C)	$P(X = 2)$	(III)	0.55
(D)	$P(X \ge 2)$	(IV)	0.15

Choose the **correct** answer from the options given below :

(1) (A) - (I), (B) - (II), (C) - (III), (D) - (IV)

(2) (A) - (IV), (B) - (III), (C) - (II), (D) - (I)

(3) (A) - (I), (B) - (II), (C) - (IV), (D) - (III)

(4) (A) - (III), (B) - (IV), (C) - (I), (D) - (II)

28. If $\sin y = x \sin(a + y)$, then $\frac{dy}{dx}$ is :

(1) $\frac{\sin^2 a}{\sin(a + y)}$

(2) $\frac{\sin(a + y)}{\sin^2 a}$

(3) $\frac{\sin(a + y)}{\sin a}$

(4) $\frac{\sin^2(a + y)}{\sin a}$

29. The unit vector perpendicular to each of the vectors $\vec{a} + \vec{b}$ and $\vec{a} - \vec{b}$, where $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ and $\vec{b} = \hat{i} + 2\hat{j} + 3\hat{k}$, is :

(1) $\frac{1}{\sqrt{6}}\hat{i} + \frac{2}{\sqrt{6}}\hat{j} + \frac{1}{\sqrt{6}}\hat{k}$

(2) $-\frac{1}{\sqrt{6}}\hat{i} + \frac{1}{\sqrt{6}}\hat{j} - \frac{1}{\sqrt{6}}\hat{k}$

(3) $-\frac{1}{\sqrt{6}}\hat{i} + \frac{2}{\sqrt{6}}\hat{j} + \frac{2}{\sqrt{6}}\hat{k}$

(4) $-\frac{1}{\sqrt{6}}\hat{i} + \frac{2}{\sqrt{6}}\hat{j} - \frac{1}{\sqrt{6}}\hat{k}$

SPACE FOR ROUGH WORK

30. The distance between the lines $\vec{r} = \hat{i} - 2\hat{j} + 3\hat{k} + \lambda(2\hat{i} + 3\hat{j} + 6\hat{k})$ and $\vec{r} = 3\hat{i} - 2\hat{j} + 1\hat{k} + \mu(4\hat{i} + 6\hat{j} + 12\hat{k})$ is :

(1) $\frac{\sqrt{28}}{7}$ (2) $\frac{\sqrt{199}}{7}$ (3) $\frac{\sqrt{328}}{7}$ (4) $\frac{\sqrt{421}}{7}$

31. If $f(x) = 2\left(\tan^{-1}(e^x) - \frac{\pi}{4}\right)$, then f(x) is :

(1) even and is strictly increasing in $(0, \infty)$

(2) even and is strictly decreasing in $(0, \infty)$

(3) odd and is strictly increasing in $(-\infty, \infty)$

(4) odd and is strictly decreasing in $(-\infty, \infty)$

32. For the differential equation $(x \log_e x)dy = (\log_e x - y)dx$

(A) Degree of the given differential equation is 1.

(B) It is a homogeneous differential equation.

(C) Solution is $2y \log_e x + A = (\log_e x)^2$, where A is an arbitrary constant

(D) Solution is $2y \log_e x + A = \log_e(\log_e x)$, where A is an arbitrary constant

Choose the **correct** answer from the options given below :

(1) (A) and (C) only (2) (A), (B) and (C) only

(3) (A), (B) and (D) only (4) (A) and (D) only

33. There are two bags. Bag-1 contains 4 white and 6 black balls and Bag-2 contains 5 white and 5 black balls. A die is rolled, if it shows a number divisible by 3, a ball is drawn from Bag-1, else a ball is drawn from Bag-2. If the ball drawn is not black in colour, the probability that it was not drawn from Bag-2 is :

(1) $\frac{4}{9}$ (2) $\frac{3}{8}$ (3) $\frac{2}{7}$ (4) $\frac{4}{19}$

34. Which of the following ***cannot*** be the direction ratios of the straight line $\frac{x-3}{2} = \frac{2-y}{3} = \frac{z+4}{-1}$?

(1) $2, -3, -1$ (2) $-2, 3, 1$

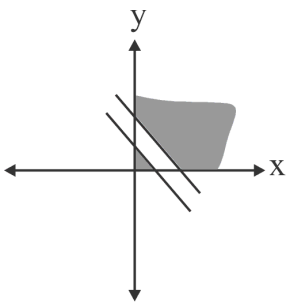
(3) $2, 3, -1$ (4) $6, -9, -3$

SPACE FOR ROUGH WORK

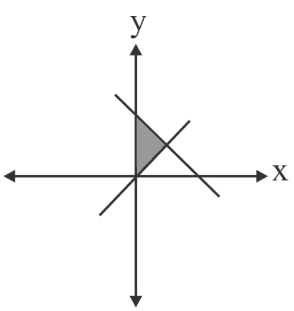
35. Which one of the following represents the correct feasible region determined by the following constraints of an LPP ?

$x + y \geq 10,\ 2x + 2y \leq 25,\ x \geq 0,\ y \geq 0$

(1)



(2)



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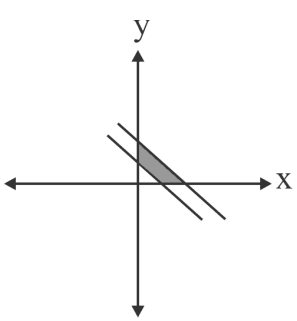
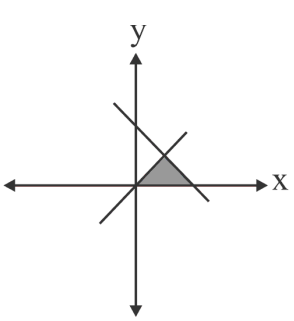


(4)



SPACE FOR ROUGH WORK

36. Let R be the relation over the set A of all straight lines in a plane such that l_1 R $l_2 \Leftrightarrow l_1$ is parallel to l_2. Then R is :

(1) Symmetric (2) An Equivalence relation

(3) Transitive (4) Reflexive

37. The probability of not getting 53 Tuesdays in a leap year is :

(1) 2/7 (2) 1/7 (3) 0 (4) 5/7

38. The angle between two lines whose direction ratios are propotional to 1, 1, -2 and $(\sqrt{3}-1)$, $(-\sqrt{3}-1)$, -4 is :

(1) $\pi/3$ (2) π (3) $\pi/6$ (4) $\pi/2$

39. If $(\vec{a}-\vec{b})\cdot(\vec{a}+\vec{b}) = 27$ and $|\vec{a}| = 2|\vec{b}|$, then $|\vec{b}|$ is :

(1) 3 (2) 2 (3) 5/6 (4) 6

40. If $\tan^{-1}\left(\dfrac{2}{3^{-x}+1}\right) = \cot^{-1}\left(\dfrac{3}{3^{x}+1}\right)$, then which one of the following is true ?

(1) There is no real value of x satisfying the above equation.

(2) There is one positive and one negative real value of x satisfying the above equation.

(3) There are two real positive values of x satisfying the above equation.

(4) There are two real negative values of x satisfying the above equation.

41. If A, B and C are three singular matrices given by $A = \begin{bmatrix} 1 & 4 \\ 3 & 2a \end{bmatrix}$, $B = \begin{bmatrix} 3b & 5 \\ a & 2 \end{bmatrix}$ and $C = \begin{bmatrix} a+b+c & c+1 \\ a+c & c \end{bmatrix}$, then the value of abc is :

(1) 15 (2) 30

(3) 45 (4) 90

SPACE FOR ROUGH WORK

42. The value of the integral $\int_{\log_e 2}^{\log_e 3} \frac{e^{2x} - 1}{e^{2x} + 1} dx$ is :

(1) $\log_e 3$
(2) $\log_e 4 - \log_e 3$
(3) $\log_e 9 - \log_e 4$
(4) $\log_e 3 - \log_e 2$

43. If $\vec{a}$, $\vec{b}$ and $\vec{c}$ are three vectors such that $\vec{a} + \vec{b} + \vec{c} = \vec{0}$, where $\vec{a}$ and $\vec{b}$ are unit vectors and $|\vec{c}| = 2$, then the angle between the vectors $\vec{b}$ and $\vec{c}$ is :

(1) 60°
(2) 90°
(3) 120°
(4) 180°

44. Let [x] denote the greatest integer function. Then match **List-I** with **List-II** :

List-I	**List-II**
(A) $\|x - 1\| + \|x - 2\|$	(I) is differentiable everywhere except at x = 0
(B) $x - \|x\|$	(II) is continuous everywhere
(C) $x - [x]$	(III) is not differentiable at x = 1
(D) $x\|x\|$	(IV) is differentiable at x = 1

Choose the **correct** answer from the options given below :

(1) (A) - (I), (B) - (II), (C) - (III), (D) - (IV)
(2) (A) - (I), (B) - (III), (C) - (II), (D) - (IV)
(3) (A) - (II), (B) - (I), (C) - (III), (D) - (IV)
(4) (A) - (II), (B) - (IV), (C) - (III), (D) - (I)

45. The rate of change (in cm^2/s) of the total surface area of a hemisphere with respect to radius r at $r = \sqrt[3]{1.331}$ cm is :

(1) 66π
(2) 6.6π
(3) 3.3π
(4) 4.4π

46. The area of the region bounded by the lines $\frac{x}{7\sqrt{3}\,a} + \frac{y}{b} = 4$, x = 0 and y = 0 is :

(1) $56\sqrt{3}\,ab$
(2) 56a
(3) ab/2
(4) 3ab

47. If A is a square matrix and I is an identity matrix such that $A^2 = A$, then $A(I - 2A)^3 + 2A^3$ is equal to :

(1) I + A
(2) I + 2A
(3) I – A
(4) A

SPACE FOR ROUGH WORK

48. Match **List-I** with **List-II** :

	List-I		**List-II**
(A)	Integrating factor of $xdy - (y + 2x^2)dx = 0$	(I)	$\frac{1}{x}$
(B)	Integrating factor of $(2x^2 - 3y)dx = xdy$	(II)	x
(C)	Integrating factor of $(2y + 3x^2)dx + xdy = 0$	(III)	x^2
(D)	Integrating factor of $2xdy + (3x^3 + 2y)dx = 0$	(IV)	x^3

Choose the **correct** answer from the options given below :

(1) (A) - (I), (B) - (III), (C) - (IV), (D) - (II)

(2) (A) - (I), (B) - (IV), (C) - (III), (D) - (II)

(3) (A) - (II), (B) - (I), (C) - (III), (D) - (IV)

(4) (A) - (III), (B) - (IV), (C) - (II), (D) - (I)

49. If the function $f : \mathbb{N} \to \mathbb{N}$ is defined as $f(n) = \begin{cases} n-1, & \text{if } n \text{ is even} \\ n+1, & \text{if } n \text{ is odd} \end{cases}$, then

(A) f is injective

(B) f is into

(C) f is surjective

(D) f is invertible

Choose the **correct** answer from the options given below :

(1) (B) only

(2) (A), (B) and (D) only

(3) (A) and (C) only

(4) (A), (C) and (D) only

50. $\int_0^{\frac{\pi}{2}} \frac{1 - \cot x}{\operatorname{cosec} x + \cos x} dx =$

(1) 0

(2) $\frac{\pi}{4}$

(3) ∞

(4) $\frac{\pi}{12}$

SPACE FOR ROUGH WORK

Section B2 (Applied Mathematics)

51. In a 700 m race, Amit reaches the finish point in 20 seconds and Rahul reaches in 25 seconds. Amit beats Rahul by a distance of :

(1) 120 m
(2) 150 m
(3) 140 m
(4) 100 m

52. For the given five values 12, 15, 18, 24, 36; the three-year moving averages are :

(1) 15, 25, 21
(2) 15, 27, 19
(3) 15, 19, 26
(4) 15, 19, 30

53. A person wants to invest an amount of ₹ 75,000. He has two options A and B yielding 8% and 9% return respectively on the invested amount. He plans to invest at least ₹ 15,000 in Plan A and at least ₹ 25,000 in Plan B. Also he wants that his investment in Plan A is less than or equal to his investment in Plan B. Which of the following options describes the given LPP to maximize the return (where x and y are investments in Plan A and Plan B respectively) ?

(1) maximize $Z = 0.08x + 0.09y$
$x \geq 15000$
$y \geq 25000$
$x + y \geq 75000$
$x \leq y$
$x, y \geq 0$

(2) maximize $Z = 0.08x + 0.09y$
$x \geq 15000$
$y \leq 25000$
$x + y \geq 75000$
$x \leq y$
$x, y \geq 0$

(3) maximize $Z = 0.08x + 0.09y$
$x \geq 15000$
$y \geq 25000$
$x + y \leq 75000$
$x \geq y$
$x, y \geq 0$

(4) maximize $Z = 0.08x + 0.09y$
$x \geq 15000$
$y \geq 25000$
$x + y \leq 75000$
$x \leq y$
$x, y \geq 0$

SPACE FOR ROUGH WORK

54. A property dealer wishes to buy different houses given in the table below with some down payments and balance in EMI for 25 years. Bank charges 6% per annum compounded monthly.

$$\left(\text{Given } \frac{(1.005)^{300} \times 0.005}{(1.005)^{300} - 1} = 0.0064 \right)$$

Property type	**Price of the property (in ₹)**	**Down Payment (in ₹)**
P	45,00,000	5,00,000
Q	55,00,000	5,00,000
R	65,00,000	10,00,000
S	75,00,000	15,00,000

Match **List-I** with **List-II** :

	List-I **Property Type**		**List-II** **EMI amount (in ₹)**
(A)	P	(I)	25,600
(B)	Q	(II)	38,400
(C)	R	(III)	32,000
(D)	S	(IV)	35,200

Choose the **correct** answer from the options given below :

(1) (A) - (I), (B) - (II), (C) - (III), (D) - (IV)

(2) (A) - (I), (B) - (III), (C) - (IV), (D) - (II)

(3) (A) - (I), (B) - (II), (C) - (IV), (D) - (III)

(4) (A) - (III), (B) - (IV), (C) - (I), (D) - (II)

SPACE FOR ROUGH WORK

55. The corner points of the feasible region for an L.P.P. are (0, 10), (5, 5), (5, 15) and (0, 30). If the objective function is $Z = \alpha x + \beta y$, $\alpha, \beta > 0$, the condition on α and β so that maximum of Z occurs at corner points (5, 5) and (0, 20) is :

(1) $\alpha = 5\beta$ (2) $5\alpha = \beta$ (3) $\alpha = 3\beta$ (4) $4\alpha = 5\beta$

56. The solution set of the inequality $|3x| \geq |6 - 3x|$ is :

(1) $(-\infty, 1]$ (2) $[1, \infty)$

(3) $(-\infty, 1) \cup (1, \infty)$ (4) $(-\infty, -1) \cup (-1, \infty)$

57. If the matrix $\begin{bmatrix} 0 & -1 & 3x \\ 1 & y & -5 \\ -6 & 5 & 0 \end{bmatrix}$ is skew-symmetric , then the value of $5x - y$ is :

(1) 12 (2) 15 (3) 10 (4) 14

58. A company is selling a certain commodity 'x'. The demand function for the commodity is linear. The company can sell 2000 units when the price is ₹ 8 per unit and it can sell 3000 units when the price is ₹ 4 per unit . The Marginal revenue at x = 5 is :

(1) ₹ 79.98 (2) ₹ 15.96

(3) ₹ 16.04 (4) ₹ 80.02

59. If the lengths of the three sides of a trapezium other than the base are 10 cm each, then the maximum area of the trapezium is :

(1) 100 cm^2 (2) $25\sqrt{3}$ cm^2

(3) $75\sqrt{3}$ cm^2 (4) $100\sqrt{3}$ cm^2

60. Three defective bulbs are mixed with 8 good ones. If three bulbs are drawn one by one with replacement, the probabilities of getting exactly 1 defective, more than 2 defective, no defective and more than 1 defective respectively are :

(1) $\frac{27}{1331}, \frac{576}{1331}, \frac{243}{1331}$ and $\frac{512}{1331}$ (2) $\frac{27}{1331}, \frac{243}{1331}, \frac{576}{1331}$ and $\frac{512}{1331}$

(3) $\frac{576}{1331}, \frac{27}{1331}, \frac{512}{1331}$ and $\frac{243}{1331}$ (4) $\frac{243}{1331}, \frac{576}{1331}, \frac{512}{1331}$ and $\frac{27}{1331}$

SPACE FOR ROUGH WORK

61. If $A = \begin{bmatrix} 2 & 4 \\ 4 & 3 \end{bmatrix}$, $X = \begin{bmatrix} n \\ 1 \end{bmatrix}$, $B = \begin{bmatrix} 8 \\ 11 \end{bmatrix}$

and AX = B, then the value of n will be :

(1) 0 (2) 1

(3) 2 (4) not defined

62. The equation of the tangent to the curve $x^{\frac{5}{2}} + y^{\frac{5}{2}} = 33$ at the point (1, 4) is :

(1) $x + 8y - 33 = 0$ (2) $12x + y - 8 = 0$

(3) $x + 8y - 12 = 0$ (4) $x + 12y - 8 = 0$

63. A random variable X has the following probability distribution :

X	– 2	– 1	0	1	2
P(X)	0.2	0.1	0.3	0.2	0.2

The variance of X will be :

(1) 0.1 (2) 1.42

(3) 1.89 (4) 2.54

64. A Multinational company creates a sinking fund by setting a sum of ₹ 12,000 annually for 10 years to pay off a bond issue of ₹ 72,000. If the fund accumulates at 5% per annum compound interest, then the surplus after paying for bond is :

(Use $(1.05)^{10} \approx 1.6$)

(1) ₹ 78,900 (2) ₹ 68,500

(3) ₹ 72,000 (4) ₹ 1,44,000

SPACE FOR ROUGH WORK

65. The least non-negative remainder when 3^{51} is divided by 7 is :

(1) 2 (2) 3 (3) 6 (4) 5

66. If $\begin{bmatrix} 5x+8 & 7 \\ y+3 & 10x+12 \end{bmatrix} = \begin{bmatrix} 2 & 3y+1 \\ 5 & 0 \end{bmatrix}$, then the value of 5x + 3y is equal to :

(1) – 1 (2) 8 (3) 2 (4) 0

67. There are 6 cards numbered 1 to 6, one number on one card. Two cards are drawn at random without replacement. Let X denote the sum of the numbers on the two cards drawn. Then P(X > 3) is :

(1) $\frac{14}{15}$ (2) $\frac{1}{15}$

(3) $\frac{11}{12}$ (4) $\frac{1}{12}$

68. Which of the following are components of a time series ?

(A) Irregular component (B) Cyclical component

(C) Chronological Component (D) Trend Component

Choose the **correct** answer from the options given below :

(1) (A), (B) and (D) only (2) (A), (B) and (C) only

(3) (A), (B), (C) and (D) (4) (B), (C) and (D) only

69. The following data is from a simple random sample :

15, 23, x, 37, 19, 32

If the point estimate of the population mean is 23, then the value of x is :

(1) 12 (2) 30 (3) 21 (4) 24

70. For an investment, if the nominal rate of interest is 10% compounded half yearly, then the effective rate of interest is :

(1) 10.25% (2) 11.25%

(3) 10.125% (4) 11.025%

SPACE FOR ROUGH WORK

71. A mixture contains apple juice and water in the ratio 10 : x. When 36 litres of the mixture and 9 litres of water are mixed, the ratio of apple juice and water becomes 5 : 4. The value of x is :

(1) 4 (2) 4.4 (3) 5 (4) 8

72. For $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, if X and Y are square matrices of order 2 such that XY = X and YX = Y, then $(Y^2 + 2Y)$ equals to :

(1) 2Y (2) I + 3X (3) I + 3Y (4) 3Y

73. A coin is tossed K times. If the probability of getting 3 heads is equal to the probability of getting 7 heads, then the probability of getting 8 tails is :

(1) $\frac{5}{512}$ (2) $\frac{45}{2^{21}}$ (3) $\frac{45}{1024}$ (4) $\frac{210}{2^{21}}$

74. If 95% confidence interval for the population mean was reported to be 160 to 170 and $\sigma = 25$, then size of the sample used in this study is :

(Given $Z_{0.025} = 1.96$)

(1) 96 (2) 125 (3) 54 (4) 81

75. Two pipes A and B together can fill a tank in 40 minutes. Pipe A is twice as fast as pipe B. Pipe A alone can fill the tank in :

(1) 1 hour (2) 2 hours

(3) 80 minutes (4) 20 minutes

76. An even number is the determinant of

(A) $\begin{bmatrix} 1 & -1 \\ -1 & 5 \end{bmatrix}$ (B) $\begin{bmatrix} 13 & -1 \\ -1 & 15 \end{bmatrix}$ (C) $\begin{bmatrix} 16 & -1 \\ -11 & 15 \end{bmatrix}$ (D) $\begin{bmatrix} 6 & -12 \\ 11 & 15 \end{bmatrix}$

Choose the **correct** answer from the options given below :

(1) (A), (B) and (D) only

(2) (A), (B) and (C) only

(3) (A), (B), (C) and (D)

(4) (B), (C) and (D) only

SPACE FOR ROUGH WORK

77. Match **List-I** with **List-II** :

	List-I **Function**		**List-II** **Derivative w.r.t. x**
(A)	$\frac{5^x}{\log_e 5}$	(I)	$5^x(\log_e 5)^2$
(B)	$\log_e 5$	(II)	$5^x\log_e 5$
(C)	$5^x\log_e 5$	(III)	5^x
(D)	5^x	(IV)	0

Choose the **correct** answer from the options given below :

(1) (A) - (I), (B) - (II), (C) - (III), (D) - (IV)

(2) (A) - (I), (B) - (III), (C) - (II), (D) - (IV)

(3) (A) - (I), (B) - (II), (C) - (IV), (D) - (III)

(4) (A) - (III), (B) - (IV), (C) - (I), (D) - (II)

78. A random variable X has the following probability distribution :

X	1	2	3	4	5	6	7
P(X)	k	2k	2k	3k	k^2	$2k^2$	$7k^2 + k$

Match the options of **List-I** to **List-II** :

	List-I		**List-II**
(A)	k	(I)	$\frac{7}{10}$
(B)	$P(X < 3)$	(II)	$\frac{53}{100}$
(C)	$P(X > 2)$	(III)	$\frac{1}{10}$
(D)	$P(2 < X < 7)$	(IV)	$\frac{3}{10}$

Choose the **correct** answer from the options given below :

(1) (A) - (I), (B) - (II), (C) - (III), (D) - (IV)

(2) (A) - (I), (B) - (III), (C) - (II), (D) - (IV)

(3) (A) - (III), (B) - (IV), (C) - (II), (D) - (I)

(4) (A) - (III), (B) - (IV), (C) - (I), (D) - (II)

SPACE FOR ROUGH WORK

79. For which one of the following purposes is CAGR (Compounded Annual Growth Rate) ***not*** used ?

(1) To calculate and communicate the average growth of a single investment

(2) To understand and analyse the donations received by a non-government organisation

(3) To demonstrate and compare the performance of investment advisors

(4) To compare the historical returns of stocks with a savings account

80. A flower vase costs ₹ 36,000. With an annual depreciation of ₹ 2,000, its cost will be ₹ 6,000 in _____ years.

(1) 10 (2) 15 (3) 17 (4) 6

81. Arun's speed of swimming in still water is 5 km/hr. He swims between two points in a river and returns back to the same starting point. He took 20 minutes more to cover the distance upstream than downstream. If the speed of the stream is 2 km/hr, then the distance between the two points is :

(1) 3 km (2) 1.5 km (3) 1.75 km (4) 1 km

82. If $e^y = x^x$, then which of the following is true ?

(1) $y\frac{d^2y}{dx^2} = 1$

(2) $\frac{d^2y}{dx^2} - y = 0$

(3) $\frac{d^2y}{dx^2} - \frac{dy}{dx} = 0$

(4) $y\frac{d^2y}{dx^2} - \frac{dy}{dx} + 1 = 0$

83. The probability of a shooter hitting a target is 3/4. How many minimum number of times must he fire so that the probability of hitting the target at least once is more than 90% ?

(1) 1 (2) 2

(3) 3 (4) 4

SPACE FOR ROUGH WORK

84. Match **List-I** with **List-II** :

	List-I		**List-II**
(A)	Distribution of a sample leads to becoming a normal distribution	(I)	Central Limit Theorem
(B)	Some subset of the entire population	(II)	Hypothesis
(C)	Population mean	(III)	Sample
(D)	Some assumptions about the population	(IV)	Parameter

Choose the **correct** answer from the options given below.

(1) (A) - (I), (B) - (II), (C) - (III), (D) - (IV)

(2) (A) - (I), (B) - (III), (C) - (IV), (D) - (II)

(3) (A) - (I), (B) - (II), (C) - (IV), (D) - (III)

(4) (A) - (III), (B) - (IV), (C) - (I), (D) - (II)

85. Ms. Sheela creates a fund of ₹ 1,00,000 for providing scholarships to needy children. The scholarship is provided in the beginning of the year. This fund earns an interest of r % per annum. If the scholarship amount is taken as ₹ 8,000, then r =

(1) $8\frac{1}{2}\%$

(2) $8\frac{16}{23}\%$

(3) $8\frac{17}{25}\%$

(4) $8\frac{2}{5}\%$

SPACE FOR ROUGH WORK

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Read carefully the following instructions :

8. No candidate will be allowed to leave the OMR Answer Sheet blank. If any OMR Answer Sheet is found blank, it shall be crossed by the Invigilator with his/her signature, mentioning "Cancelled" on it.

9. Do not tear or fold any page of the Test Booklet and OMR Answer Sheet.

10. Candidates are advised to ensure that they fill the correct particulars on the OMR Answer Sheet, i.e., Application No., Roll No., Test Booklet No., Name, Mother's Name, Father's Name and Signature.

11. Rough work is to be done in the space provided for this purpose in the Test Booklet only.

12. The answers will be evaluated through electronic scanning process. Incomplete or incorrect entries may render the OMR Answer Sheet invalid.

13. Candidates are advised not to fold or make any stray marks on the OMR Answer Sheet. Use of Eraser, Nail, Blade, White Fluid/Whitener, etc., to smudge, scratch or damage in any manner the OMR Answer Sheet during examination is strictly prohibited. Candidature and OMR Answer Sheet of candidates using Eraser, Nail, Blade or White Fluid/Whitener to smudge, scratch or damage in any manner shall be cancelled.

14. There will be one copy of OMR Answer Sheet i.e., the Original Copy. After the examination is over, the candidate shall hand over the OMR Answer Sheet to the Invigilator. The candidate can take away the Test Booklet after the examination is over. If the candidate does not hand over the OMR Answer Sheet to the Invigilator and goes away with the OMR Answer Sheet, his/her candidature shall be cancelled and criminal proceedings shall also be initiated against him/her.

15. Candidates are advised strictly not to carry handkerchief, any mobile phone, any type of watch, belt or wear ornaments like ring, chain, ear-ring, etc., electronic or communication device, pen, pencil, eraser, sharpener and correction fluid to the Examination Centre. If any candidate is found possessing any such item, he/she will not be allowed to enter the examination centre. Possession of a mobile phone or any other aiding material as mentioned above by the candidate in the examination room will be treated as a serious violation and it may lead to cancellation of the candidature and debarring him/her from future examinations.

16. If a candidate violates any instructions or shows any indiscipline or misbehaviour, appropriate action will be taken including cancellation of candidature and debarring from future examinations.

17. Use of electronic/manual calculator is **not** allowed.