

DU MA Economics

Topic:- ECO MA

- 1) Consider the problem of maximizing $f(x, y) = x^2 + 2xy + by^2$, with respect to x, y and subject to the constraint $x + y = 100$, where b is a parameter taking some fixed value greater than 1. Let $v(b)$ the minimum value attained, as a function of b . Let $v'(b)$ the derivative of $v(b)$. Which of the following is correct?

[Question ID = 10993]

1. $v'(b) > 0$

[Option ID = 43969]

2. $v'(b) < 0$

[Option ID = 43970]

3. $v'(b) = 0$

[Option ID = 43971]

4. The sign of $v'(b)$ changes with b

[Option ID = 43972]

- 2) Consider any real valued, continuous function f , defined on the set of all real numbers, satisfying $f(f(x)) = x$ for all $x \in \mathfrak{R}$ (set of all real numbers). If f is not the identity function, then which of the following is true?

[Question ID = 10994]

1. f is a constant function

[Option ID = 43973]

2. f is a strictly decreasing function

[Option ID = 43974]

3. f is a strictly increasing function

[Option ID = 43975]

4. No function other than the identity function can satisfy this property

[Option ID = 43976]

- 3) Consider a real-valued function f that satisfies $f'(x) = (f(x))^2$, for all x in some domain of real numbers, and also satisfies $f(2) = 2$. Find $f(-2)$.

[Question ID = 10995]

1. $\frac{2}{3}$

[Option ID = 43977]

2. $-\frac{2}{3}$

[Option ID = 43978]

3. $\frac{2}{7}$

[Option ID = 43979]

4. $-\frac{2}{7}$

[Option ID = 43980]

- 4) Find the value of $\sum_{r=0}^{50} \binom{100}{2r}$.

Notation: $\binom{a}{b}$ denotes a choose b

[Question ID = 10996]

1. 2^{99}

[Option ID = 43981]

2. 2^{100}

[Option ID = 43982]

3. 2^{101}

[Option ID = 43983]

4. 2^{51}

[Option ID = 43984]

5) Suppose that n participants with distinct names arrive for a conference. The organizers have prepared name-tags for all of them, but by mistake, allocate the name-tags randomly to the participants. What is the expected number of participants who will receive their own name-tag?

[Question ID = 10997]

1. $\frac{n}{2}$

[Option ID = 43985]

2. $\frac{n}{(n-2)}$

[Option ID = 43986]

3. 1

[Option ID = 43987]

4. $\frac{(n-1)}{n}$

[Option ID = 43988]

6) A right angled triangle has two equal sides of 1 inch. One of these sides, drawn horizontally, is divided into $(n + 1)$ equal portions. On each portion after the first, a rectangle is formed with height equal to the vertical distance from the left-hand end portion of the hypotenuse of the triangle. Find the sum of rectangle areas (S) and its limiting value.

[Question ID = 10998]

1. $S = \frac{n}{n+1}$ and the limit is 1

[Option ID = 43989]

2. $S = \frac{n}{2(n+1)}$ and the limit is $\frac{1}{2}$

[Option ID = 43990]

3. $S = \frac{n+2}{n+1}$ and the limit is 1

[Option ID = 43991]

4. $S = \frac{n+2}{2(n+1)}$ and the limit is $\frac{1}{2}$

[Option ID = 43992]

7) If $|x| < 1$ and $y = \sum_{k=1}^{\infty} (-1)^{(k+1)} \frac{x^k}{k}$, then which of the following is true?

If $|x| < 1$ and $y = \sum_{k=1}^{\infty} (-1)^{(k+1)} \frac{x^k}{k}$, then which of the following is true?

Notation: $|x|$ denotes modulus of x and $k!$ is the factorial of k .

[Question ID = 10999]

1. $x = \sum_{k=1}^{\infty} (-1)^k \frac{y^k}{k}$

[Option ID = 43993]

2. $x = \sum_{k=1}^{\infty} \frac{k}{y^k}$

[Option ID = 43994]

3. $x = \sum_{k=1}^{\infty} \frac{y^k}{k!}$

[Option ID = 43995]

4. $x = \sum_{k=1}^{\infty} (-1)^k \frac{y^k}{k!}$

[Option ID = 43996]

8) Consider the vector space $\mathcal{R}^n$ for some $n \geq 2$, over the field of real numbers; and the following two statements:

A: $\{v_1, v_2, \dots, v_{n-1}, v_n\}$ are linearly independent vectors.

B: $\{(v_1 + v_2), (v_2 + v_3), \dots, (v_{n-1} + v_n), (v_n + v_1)\}$ are linearly independent vectors.

Which of the following statements is true?

[Question ID = 11000]

1. A implies B and B implies A.

[Option ID = 43997]

2. A implies B if n is odd, and B always implies A.

[Option ID = 43998]

3. A implies B if n is even, and B always implies A.

[Option ID = 43999]

4. A always implies B and B implies A if n is even.

[Option ID = 44000]

- 9) Consider the following system of equations in the unknowns x_1, x_2, x_3 , with λ being a real parameter.

$$x_1 + 2x_2 - 2x_3 = 0$$

$$2x_1 - x_2 + \lambda x_3 = 0$$

$$3x_1 + x_2 - x_3 = 0$$

Under which of the following conditions, this system has nonzero solutions?

[Question ID = 11001]

1. For both positive and negative values of λ

[Option ID = 44001]

2. For more than one positive values of λ

[Option ID = 44002]

3. For $\lambda = 1$

[Option ID = 44003]

4. For more than one negative values of λ

[Option ID = 44004]

- 10) There are four statements. Which of these are true?

Statement 1: $\{y \text{ is a rational number} \mid -200 \leq y \leq 200\}$ is a countable set.

Statement 2: $\{y = \frac{m}{n} \mid m \text{ and } n \text{ are integers}\}$ is an uncountable set.

Statement 3: $\{y \text{ is a real number} \mid 0 \leq y < 0.7\}$ is an uncountable set.

Statement 4: $\{y = \frac{\sqrt{2}}{n} \mid n \text{ is a positive integer}\}$ is an uncountable set

[Question ID = 11002]

1. Statement 1 and Statement 2

[Option ID = 44005]

2. Statement 1 and Statement 3

[Option ID = 44006]

3. Statement 2 and Statement 4

[Option ID = 44007]

4. Statement 3 and Statement 4

[Option ID = 44008]

- 11) If $x^2 + y^2 + z^2 = 1$, then what is the maximum value of $(-x + z)$?

[Question ID = 11003]

1. 1

[Option ID = 44009]

2. $\sqrt{2}$

[Option ID = 44010]

3. $\sqrt{3}$

[Option ID = 44011]

4. It has no maximum

[Option ID = 44012]

- 12) Consider a triangle with sides $AC = 2$, $AB = \sqrt{3}$ and $BC = 1$. Choose a random point, P , inside the triangle. Minimum distance from P to AC , AB and BC are D_1 , D_2 , and D_3 respectively. Find $2D_1 + \sqrt{3}D_2 + D_3$.

[Question ID = 11004]

1. $\sqrt{3}$

[Option ID = 44013]

2. $3 + \sqrt{3}$

[Option ID = 44014]

3. $3\sqrt{3}$

[Option ID = 44015]

4. $3 - \sqrt{3}$

[Option ID = 44016]

- 13) One girl is training for half marathon in Delhi. She decides to run x_i kilometre on i^{th} day for next 12 days (that is x_1 kilometre on day 1, x_2 kilometre on day 2 etc.). On the last day she finds that she trained for 12 kilometre per day on an average. Which of the following statements is true?

[Question ID = 11005]

1. $\sum_{i=1}^{12} \log_{12} x_i < 12$

[Option ID = 44017]

2. $\sum_{i=1}^{12} \log_{12} x_i > 12$

[Option ID = 44018]

3. $\sum_{i=1}^{12} \log_{12} x_i = 12$

[Option ID = 44019]

4. $\sum_{i=1}^{12} \log_{12} x_i = 12^{12}$

[Option ID = 44020]

- 14) Three boxes are presented to a contestant. Exactly one box has an expensive gift and the other two are empty. Each box has imprinted on it a declaration. The declarations are as follows:

Box 1: The gift is not here

Box 2: The gift is not here

Box 3: The gift is in Box 2

A declaration can be either true or false. Find the least number of true declarations that allows the contestant to logically deduce the gift-box?

[Question ID = 11006]

1. 0

[Option ID = 44021]

2. 1

[Option ID = 44022]

3. 2

[Option ID = 44023]

4. 3

[Option ID = 44024]

- 15) Let $a_1, a_2, a_3 \dots a_n$ are real numbers such that $a_1 + a_2 + a_3 + \dots + a_n = 0$. Suppose $n \geq 5$. Which of the following statements is true about the roots of $q(x) = a_1 + 2a_2x + 3a_3x^2 + \dots + na_nx^{(n-1)}$?

[Question ID = 11007]

1. $q(x)$ has at least one real root

[Option ID = 44025]

2. $q(x)$ has no real root
[Option ID = 44026]
3. $q(x)$ has $(n - 1)$ real roots
[Option ID = 44027]
4. $q(x)$ has $(n - 2)$ real roots
[Option ID = 44028]

16) Which of the following statements is true?

[Question ID = 11008]

1. Any preference can be represented by a utility function
[Option ID = 44029]
2. Any complete and transitive preference can be represented by a utility function
[Option ID = 44030]
3. Some complete and transitive preferences cannot be represented by a utility function
[Option ID = 44031]
4. Any complete and monotonic preference can be represented by a utility function
[Option ID = 44032]

17) Ms A likes grapes (G) and strawberries (S). With every two pieces of grapes, she prefers eating three pieces of strawberries. Thus consumed, every piece of grape gives her a utility level of 1. Income of Ms A is given by I . Per piece price of grapes and strawberries are given by $p_G = 3$ and $p_S = 2$ respectively. Suppose price of strawberries change to $p_S = 3$. What should be the change in income (ΔI) to maintain the same level of utility?

[Question ID = 11009]

1. $\Delta I = \frac{5I}{4}$
[Option ID = 44033]
2. $\Delta I = -\frac{5I}{4}$
[Option ID = 44034]
3. $\Delta I = \frac{I}{4}$
[Option ID = 44035]
4. $\Delta I = -\frac{I}{4}$
[Option ID = 44036]

18) Suppose that commodity prices are strictly positive. Consider the following utility functions. One of these utility functions has no income effect on good X for a certain range of income. Identify it.

[Question ID = 11010]

1. $u(x, y) = \ln x + y$
[Option ID = 44037]
2. $u(x, y) = \ln x + \ln y$
[Option ID = 44038]
3. $u(x, y) = \sqrt{xy}$
[Option ID = 44039]
4. $u(x, y) = \min\{x, y\}$
[Option ID = 44040]

19) A Rotating Credit and Savings Association (ROSCA) is made up of a group of individuals. Members of a ROSCA pool their money into a common fund, generally structured around monthly contributions, and a single member withdraws the money from it as a lump sum (called the 'pot') at the end of each quarter. In one cycle, each member must withdraw the pot exactly once.

ROSCA is quite common in the developing countries. It is an example of:

[Question ID = 11011]

1. Public good
[Option ID = 44041]
2. Moral hazard
[Option ID = 44042]
3. Risk sharing

[Option ID = 44043]

4. Altruism

[Option ID = 44044]

- 20) An economy consists of two agents (R and P) and two states (pandemic and normal). If the state is pandemic then R earns 10 and P earns 5, while in normal state R earns 20 and P earns 10. Probability of pandemic is known; it is denoted by q ; $0 < q < 1$. Utility function of both R and P is given by $u(x)$, where x is the net earning. Both P and R are risk averse.

An insurance company, is selling an 'actuarially fair' 'pandemic insurance' where the consumer has the same income irrespective of the state (pandemic or normal). Actuarially fair plans are those insurance plans where the insurance company makes no profit. Also note that the insurance company is risk neutral.

Consider the following schemes to protect P in case of pandemic:

Scheme A: The government purchases a 'pandemic insurance' for P . Premium of the 'pandemic insurance' is collected from R as tax.

Scheme B: If the state is pandemic then R pays 5 to P through a charity, otherwise in normal state there is no transfer.

Which of the above schemes will R prefer? You may also assume that R is not eligible to buy the pandemic insurance.

[Question ID = 11012]

1. Scheme A will be preferred by R

[Option ID = 44045]

2. Scheme B will be preferred by R

[Option ID = 44046]

3. R will be indifferent

[Option ID = 44047]

4. Depends on the functional form of u

[Option ID = 44048]

- 21) Suppose that the market for pizza is perfectly competitive with constant long run marginal cost. If there is a per unit sales tax on pizza then which of the following is correct?

[Question ID = 11013]

1. Producers will bear all the taxation burden

[Option ID = 44049]

2. Consumers will bear all the taxation burden

[Option ID = 44050]

3. Consumers and producers will equally share the taxation burden

[Option ID = 44051]

4. Tax incidence will depend on the shape of the demand curve

[Option ID = 44052]

- 22) Suppose a monopolist produces oil in one factory but sells oil in two cities. In each city the monopolist faces the same inverse demand function $p = f(q)$, such that f is strictly decreasing and strictly concave. Cost function is increasing and convex in quantity. She sells q_1 units in city A and q_2 units in city B per month where $q_1 < q_2$. Which of the following choices will increase her profit?

[Question ID = 11014]

1. Sell $(q_1 + q_2)$ units per month in city B and nothing in city A

[Option ID = 44053]

2. Sell $(q_1 + q_2)$ units per month in city A and nothing in city B

[Option ID = 44054]

3. Sell $\frac{q_1 + q_2}{2}$ units per month in each city

[Option ID = 44055]

4. Sell q_2 units per month in city A and q_1 units per month in city B

[Option ID = 44056]

23) Two buyers bid for a single object in an auction. Valuation of a buyer is private information. However it is known that each of them independently draw their valuations from the

$Uniform[0, 1]$ distribution. The auction rule lets the highest bidder take the object by paying the lowest bid. Suppose that the buyers bid truthfully, that is bid of a buyer is equal to her valuation of the object. Find the expected revenue of the auction.

[Question ID = 11015]

1. $\frac{1}{3}$

[Option ID = 44057]

2. $\frac{2}{3}$

[Option ID = 44058]

3. $\frac{1}{2}$

[Option ID = 44059]

4. 1

[Option ID = 44060]

24) The competitive market for good X has the demand function $x^d = 100 - p$ and the supply function $x^s = 20 + 3p$. If the government imposes a sales tax of Rs 10 per unit of the good on sellers, the equilibrium market price will increase by:

[Question ID = 11016]

1. Rs. 10

[Option ID = 44061]

2. Rs. 7.50

[Option ID = 44062]

3. Rs. 5

[Option ID = 44063]

4. Rs. 0

[Option ID = 44064]

25)

A monopolist sells hand embroidered Pashmina shawls to two types of customers: 'Rich' and 'Middle Income'. 'Rich' customers value at most two shawls; first shawl at Rs. 50 thousands and the marginal value of second shawl is Rs. 30 thousands. 'Middle Income' customers want at most one shawl and they value it at Rs. 35 thousands. There are 50 identical 'Rich' and 100 identical 'Middle Income' customers. Cost of production is Rs. 25 thousands per shawl.

Suppose that the monopolist can **NOT** distinguish between a 'Rich' and a 'Middle Income' customer. She, however, decided to adopt the following scheme. If a customer purchases two shawls then the package is priced at p_2 , whereas if a customer purchases one shawl, she pays p_1 . What are the profit maximizing prices?

Suppose that the monopolist can NOT distinguish between a 'Rich' and a 'Middle Income' customer. She, however, decided to adopt the following scheme. If a customer purchases two shawls then the package is priced at , whereas if a customer purchases one shawl, she pays . What are the profit maximizing prices?

[Question ID = 11017]

1. $p_1 = 35,000$ and $p_2 = 65,000$

[Option ID = 44065]

2. $p_1 = 35,000$ and $p_2 = 50,000$

[Option ID = 44066]

3. $p_1 = 25,000$ and $p_2 = 65,000$

[Option ID = 44067]

4. $p_1 = 50,000$ and $p_2 = 80,000$

[Option ID = 44068]

26)

Suppose that 'ABC Cinemas' is the monopolist in a town. Demand to see a movie in that town is given by $Q = (100 - 10p)$ in the afternoon and $Q = (200 - 10p)$ in the evening, where p denotes the price of a ticket. Currently the movie distributor charges Rs. 4 per ticket sold by the 'ABC Cinemas'. Suppose that the distributor instead asks the 'ABC Cinemas' to pay a flat fee of Rs. X to show the movie, with no charge per customer. Find the value of X such that 'ABC Cinemas' will be indifferent between the current 'pay per ticket' contract and the 'fixed pay' contract. Assume that 'ABC Cinemas' does not incur any cost other than their payment to the distributor.

[Question ID = 11018]

1. 'Pay per ticket' contract is always better

[Option ID = 44069]

2. 'Fixed pay' contract is always better

[Option ID = 44070]

3. $X = 520$

[Option ID = 44071]

4. $X = 180$

[Option ID = 44072]

27)

In an exchange economy there are two goods X and Y and two agents A and B. A owns 10 units of good Y while B owns 10 units of good X . A has a lexicographic preference where good X comes before good Y . She will choose the bundle that offers the most X , no matter how much Y there is. Only when there is a tie between bundles with regard to X will A start comparing Y across bundles. Agent B also has lexicographic preference, but for her good Y comes before good X . Consider the following statements.

Statement I: An allocation where A gets 10 units of good X and B gets 10 units of good Y is Pareto optimal.

Statement II: An allocation where A gets 10 units of good X and 5 units of good Y while B gets 5 units of good Y is Pareto optimal.

Choose the **correct** answer from the options given below.

[Question ID = 11019]

1. Both Statement I and Statement II are true

[Option ID = 44073]

2. Both Statement I and Statement II are false

[Option ID = 44074]

3. Statement I is true but Statement II is false

[Option ID = 44075]

4. Statement I is false but Statement II is true

[Option ID = 44076]

28) Which of the following assumptions is **NOT** required for the 'First welfare theorem' in an exchange economy?

[Question ID = 11020]

1. Well defined property rights

[Option ID = 44077]

2. Absence of externalities

[Option ID = 44078]

3. Monotonic preferences

[Option ID = 44079]

4. Convex preferences

[Option ID = 44080]

29)

Two players must independently and simultaneously decide how much to donate to a charity organization. Each has a budget of Rs. 200. Whenever the charity receives at least Rs 100 in aggregate (irrespective of the identity of the donor), each player enjoys a payoff equivalent to Rs. 60. This captures the fact that they are somewhat altruistic. Additional aggregate donation

(above Rs. 100) does not bring any extra payoff. All payoffs are calculated in money terms. For example, if the first player donates Rs. x and the second player donates Rs. y , then the payoff of first player is

$$\begin{aligned} &[(200 - x) + 60] \text{ if } (x + y) \geq 100 \\ &(200 - x) \text{ if } (x + y) < 100 \end{aligned}$$

Which of the following is true?

[Question ID = 11021]

1. This game has no Nash equilibrium in pure strategies

[Option ID = 44081]

2. This game has only one Nash equilibrium in pure strategies

[Option ID = 44082]

3. This game has many Nash equilibriums in pure strategies, where the aggregate donation is less than 100

[Option ID = 44083]

4. This game has many Nash equilibriums in pure strategies, where the aggregate donation is Rs. 100

[Option ID = 44084]

30)

Two players must independently and simultaneously decide how much to donate to a charity organization. Each has a budget of Rs. 200. Whenever the charity receives at least Rs 100 in aggregate (irrespective of the identity of the donor), each player enjoys a payoff equivalent to Rs. 60. This captures the fact that they are somewhat altruistic. Additional aggregate donation (above Rs. 100) does not bring any extra payoff. All payoffs are calculated in money terms. For example, if the first player donates Rs. x and the second player donates Rs. y , then the payoff of first player is

$$\begin{aligned} &[(200 - x) + 60] \text{ if } (x + y) \geq 100 \\ &(200 - x) \text{ if } (x + y) < 100 \end{aligned}$$

Which of the following is **NOT** true?

[Question ID = 11022]

1. Each player has at least one weakly dominated strategy

[Option ID = 44085]

2. Each player has at least one strictly dominated strategy

[Option ID = 44086]

3. Each player has a strategy which weakly dominates all other strategies

[Option ID = 44087]

4. Maximin payoff of each player is 200

[Option ID = 44088]

31)

Consider the hypothetical economy with aggregate production function given by $F(L, K) = L^{2/3}K^{1/3}$, and 10 percent annual rate of depreciation. Find the 'golden rule' level of capital stock for this economy. Notation: L, K denote labour and capital respectively

[Question ID = 11023]

1. $(10/3)^{3/2}$

[Option ID = 44089]

2. $\frac{1}{2}$

[Option ID = 44090]

3. $(10/3)^{1/2}$

[Option ID = 44091]

4. $(3/10)^{3/2}$

[Option ID = 44092]

32) Given below are two statements

Statement I: 'Balanced Growth' in the Solow model implies identical rates of growth in different sectors of the economy.

Statement II: 'Balanced Growth' in the Solow model implies constant factor shares in a growing economy.

Choose the *correct* answer from the options given below

[Question ID = 11024]

1. Both Statement I and Statement II are true

[Option ID = 44093]

2. Both Statement I and Statement II are false

[Option ID = 44094]

3. Statement I is true but Statement II is false

[Option ID = 44095]

4. Statement I is false but Statement II is true

[Option ID = 44096]

- 33) Suppose an economy can produce e^k amount of output per capita if it uses k amount of capital per capita. Which of the following is correct?

[Question ID = 11025]

1. The economy has a stable steady state equilibrium

[Option ID = 44097]

2. The economy has multiple stable steady state equilibria

[Option ID = 44098]

3. The economy has unique steady state equilibrium

[Option ID = 44099]

4. There may not be a steady state equilibrium

[Option ID = 44100]

- 34) Consider a small open economy, where domestic and foreign prices are normalised, M is money supply, L is money demand, i is domestic interest rate, i^* is foreign interest rate, Y is output, A is aggregate spending by domestic residents on consumption and investment, G is government expenditure, X is net exports, E is exchange rate (domestic currency per unit of foreign currency), B is Balance of Payments, KI is net capital inflows.

$$M = L(i, Y)$$

$$Y = A(i, Y) + G + X(Y, E)$$

$$B = 0 = KI(i - i^*) + X(Y, E)$$

Assume that for this economy domestic and foreign assets are perfect substitutes for each other, there is no arbitrage in equilibrium, it operates under flexible exchange rate regime and Marshall Lerner condition holds. What will be the impact of an increase in government spending on imported goods?

[Question ID = 11026]

1. Rise in domestic interest rate and output

[Option ID = 44101]

2. Rise in domestic output but domestic interest rate remains unchanged

[Option ID = 44102]

3. Both domestic output and interest rate remain unchanged

[Option ID = 44103]

4. Rise in domestic interest rate but domestic output remains unchanged

[Option ID = 44104]

35)

The aggregate wage bill in an economy is equal to 40 and output, which is produced according to the Cobb-Douglas production function, is equal to 100. The output growth rate is 10 percent and the growth rates of capital and labor are 10 percent and 5 percent respectively. What is the overall productivity (TFP) growth rate for this economy?

[Question ID = 11027]

1. 0.03

[Option ID = 44105]

2. 0.02

[Option ID = 44106]

3. **0.04**

[Option ID = 44107]

4. **0.01**

[Option ID = 44108]

36)

The Phillips curve relation for an economy is given by $\pi_t - \pi_t^e = 0.1 - 3u_t$ where $\pi_t^e = \pi_{t-1}$. Suppose inflation in year $(t - 1)$ is 2 percent. In year t , the central bank decides to keep the unemployment rate at 3 percent forever. Find the rate of inflation for years t , $t + 1$, $t + 2$ and $t + 3$?

Notation: Actual rate of inflation at period t is π_t ; expected rate of inflation at period t is π_t^e ; rate of unemployment at period t is u_t .

[Question ID = 11028]

1. **1%, 2%, 3% and 4%** respectively

[Option ID = 44109]

2. **2%, 3%, 4% and 5%** respectively

[Option ID = 44110]

3. **3%, 4%, 5% and 6%** respectively

[Option ID = 44111]

4. **2%, 4%, 5% and 6%** respectively

[Option ID = 44112]

37) If government finances its expenditure with taxes then which of the following is correct?[Question ID = 11029]

1. It causes both reserves and the monetary base to rise. [Option ID = 44113]
2. It causes both reserves and the monetary base to decline. [Option ID = 44114]
3. It causes reserves to rise, but the monetary base to decline. [Option ID = 44115]
4. It has no net effect on the monetary base. [Option ID = 44116]

38)

Consider the following economy:

$$C = 0.8(1 - \tau)Y$$

$$\tau = 0.25$$

$$I = 900 - 50r$$

$$\bar{G} = 800$$

$$L = 0.25Y - 62.5r$$

$$\frac{\bar{M}}{P} = 500$$

Aggregate consumption is C ; average rate of tax on income is τ ; aggregate income is Y ; aggregate investment is I ; average rate of interest is r ; autonomous government expenditure is $\bar{G}$; aggregate demand for money is L ; real money supply in the economy is $\frac{\bar{M}}{P}$.

Find the equilibrium rate of interest in this economy.

[Question ID = 11030]

1. **$r = 5$**

[Option ID = 44117]

2. **$r = 6$**

[Option ID = 44118]

3. **$r = 7$**

[Option ID = 44119]

4. **$r = 8$**

[Option ID = 44120]

39)

Consider the following economy:

$$C = 0.8(1 - \tau)Y$$

$$\tau = 0.25$$

$$I = 900 - 50r$$

$$I = 900 - 50r$$

$$\bar{G} = 800$$

$$L = 0.25Y - 62.5r$$

$$\frac{\bar{M}}{P} = 500$$

Aggregate consumption is C ; average rate of tax on income is τ ; aggregate income is Y ; aggregate investment is I ; average rate of interest is r ; autonomous government expenditure is $\bar{G}$; aggregate demand for money is L ; real money supply in the economy is $\frac{\bar{M}}{P}$.

Find the equilibrium aggregate income in this economy.

[Question ID = 11031]

1. $Y = 3000$

[Option ID = 44121]

2. $Y = 3500$

[Option ID = 44122]

3. $Y = 4000$

[Option ID = 44123]

4. $Y = 4500$

[Option ID = 44124]

40)

There are two countries, X and Y . Both have the same production function. The two countries start out with the same levels of capital, labour and technology and the capital-labour ratio is lower than the steady state level of capital per person. X has a saving rate of 30 percent, whereas Y has a saving rate of 25 percent. In both countries, the growth rate of population is 3 percent per year, depreciation rate is equal to 5 percent per year and rate of technical progress equals 3 percent per year. According to the Solow growth model, which of the following statements are correct?

[Question ID = 11032]

1. Y will exhibit higher growth rate of output per person in the short-run and output will grow at 6% per year in both countries in the steady state.

[Option ID = 44125]

2. X will exhibit higher growth rate of output per person in the short-run and output will grow at 6% per year in both countries in the steady state

[Option ID = 44126]

3. Both X and Y will exhibit same growth rate of output per person in the short-run and output will grow at 8% per year in both countries in the steady state.

[Option ID = 44127]

4. X will exhibit higher growth rate of output per person in the short-run and output will grow at 8% per year in both countries in the steady state

[Option ID = 44128]

41)

Suppose X is a random variable which takes values in the interval $[-\frac{1}{2}, \frac{1}{2}]$. The probability distribution function is denoted by $\Phi(x)$. Which of the following is certainly true?

[Question ID = 11033]

1. For any real numbers a, b with $b > a$, $\Phi(b) > \Phi(a)$

[Option ID = 44129]

2. For any real numbers a, b in the interval $[-\frac{1}{2}, \frac{1}{2}]$ with $b > a$, $\Phi(b) > \Phi(a)$

[Option ID = 44130]

3. Expectation of X equals 0

[Option ID = 44131]

4. Variance of X cannot exceed 1

[Option ID = 44132]

42) Which of the following statements is correct:

[Question ID = 11034]

1. A large sample (say 1000 observations) is always representative of the population

[Option ID = 44133]

2. The observed significance level (P-value) of a test depends on the data

[Option ID = 44134]

3. Sample mean does not vary from sample to sample

[Option ID = 44135]

4. Standard Deviation and Standard Error is one and the same thing

[Option ID = 44136]

43)

You have three variables Y, X_1, X_2 . First you regress (OLS) Y on X_1 and X_2 to get the regression coefficients corresponding to X_1 and X_2 as b_1 and b_2 respectively. Then you also regress (OLS) Y on X_1 and $X_1 + X_2$ to get the regression coefficients corresponding to X_1 and $X_1 + X_2$ as c_1 and c_2 respectively. Which of the following statements is correct?

[Question ID = 11035]

1. There is no need to run the second regression; c_1 and c_2 can be derived from b_1 and b_2 directly

[Option ID = 44137]

2. It is incorrect to run the second regression; it will not give an unbiased estimator

[Option ID = 44138]

3. It is better to run the first regression; Sum of Square of Residuals in the first regressions will be smaller than that of the second regression

[Option ID = 44139]

4. It is incorrect to run the second regression, the error term will be correlated with independent variables

[Option ID = 44140]

- 44) Suppose we run OLS regression: $Y_i = \alpha + \beta X_i + \epsilon_i$, where notations have their usual meaning. After this we get an estimate of $\hat{Y}_i = \hat{\alpha} + \hat{\beta} X_i$. Now we regress (OLS) Y_i on $\hat{Y}_i$. Estimated coefficient of $\hat{Y}_i$ is $\hat{\gamma}$. Which of the following is correct?

[Question ID = 11036]

1. $\hat{\gamma} = \hat{\alpha}$

[Option ID = 44141]

2. $\hat{\gamma} = \hat{\beta}$

[Option ID = 44142]

3. $\hat{\gamma} = 0$

[Option ID = 44143]

4. $\hat{\gamma} = 1$

[Option ID = 44144]

45)

Let X_1, X_2 and X_3 are three (pairwise) uncorrelated random variables. The mean and variance of each variable is 0 and 3, respectively. Find the correlation between $(X_1 + X_2)$ and $(X_1 + X_3)$.

[Question ID = 11037]

1. 0

[Option ID = 44145]

2. $\frac{1}{2}$

[Option ID = 44146]

3. $\frac{1}{3}$

[Option ID = 44147]

4. 1

[Option ID = 44148]

46)

X and Y are jointly normally distributed. Suppose for any real number x , the conditional

expectation of Y given $X = x$ is 0. Note that for any function $g : \mathfrak{R}^2 \mapsto \mathfrak{R}$,

- $E[g(Y, X)|X]$ is a random variable
- If $g(Y, X) \equiv u(X)v(Y)$ for some function $u : \mathfrak{R} \mapsto \mathfrak{R}$ and some function $v : \mathfrak{R} \mapsto \mathfrak{R}$, then $E[g(Y, X)|X] = u(X) \cdot E[v(Y)|X]$
- $E[g(Y, X)] = E[E[g(Y, X)|X]]$

E denotes expectation. Which of the following statements is true?

[Question ID = 11038]

1. $E[Y] = 0$ but $E[YX] \neq 0$

[Option ID = 44149]

2. $E[Y] = 0, E[YX] = 0$ but $E[YX^2] \neq 0$

[Option ID = 44150]

3. $E[Y] = 0, E[YX] = 0$ and $E[YX^2] = 0$

[Option ID = 44151]

4. $E[Y] = 0, E[YX] = 0, E[YX^2] = 0$ and $E[(YX)^2] = 0$

[Option ID = 44152]

47)

An urn contains 2 blue balls and 10 red balls. Red balls are numbered 1, 2, ..., 10. Blue balls are not numbered. Balls are randomly drawn from the urn and returned until a blue ball is obtained at which point the experiment stops. Find the probability that ball number 9 is drawn at least once.

[Question ID = 11039]

1. $\frac{1}{12}$

[Option ID = 44153]

2. $\frac{1}{10}$

[Option ID = 44154]

3. $\frac{1}{4}$

[Option ID = 44155]

4. $\frac{1}{3}$

[Option ID = 44156]

48) A fair coin is tossed until a head comes up for the first time. Find the probability of this happening on an odd-numbered toss. [Question ID = 11040]

1. $\frac{1}{2}$

[Option ID = 44157]

2. $\frac{1}{3}$

[Option ID = 44158]

3. $\frac{2}{3}$

[Option ID = 44159]

4. $\frac{3}{4}$

[Option ID = 44160]

49) Which of the following statements is true about Exponential probability distribution? [Question ID = 11041]

1. Mean and median are the same [Option ID = 44161]
2. The mean is greater than the median [Option ID = 44162]
3. The mean is smaller than the median [Option ID = 44163]
4. Mean and median cannot be compared - it depends on parameters [Option ID = 44164]

50)

The cumulative distribution function $F(x)$ of a random variable has a slope of 2 for x in the interval $[0, 0.5]$ and takes a constant value thereafter. Which of the following statements most accurately defines the probability density function of this random variable?

[Question ID = 11042]

1. It is constant in the interval $[0, 0.5]$ and zero outside

[Option ID = 44165]

2. It is zero for all x outside $[0, 2]$ and 0.5 for all values inside it

[Option ID = 44166]

3. It is increasing in the $[0, 0.5]$ interval and constant and positive for all higher values of x

[Option ID = 44167]

4. It is increasing in the interval $[0, 0.5]$ and zero for all higher values of x

[Option ID = 44168]

